## Missouri Educator Gateway Assessments

## FIELD 012: MIDDLE SCHOOL EDUCATION: MATHEMATICS TEST FRAMEWORK

January 2014

## DRAFT

| Content Domain | Range of <br> Competencies | Approximate <br> Percentage of <br> Test Score |
| :--- | :---: | :---: |
| I. Number and Operations | $0001-0002$ | $19 \%$ |
| II. Algebra and Functions | $0003-0006$ | $36 \%$ |
| III. Measurement and Geometry | $0007-0009$ | $27 \%$ |
| IV. Statistics and Probability | $0010-0011$ | $18 \%$ |

# Missouri Educator Gateway Assessments TEST FRAMEWORK <br> FIELD 012: MIDDLE SCHOOL EDUCATION: MATHEMATICS 

A scientific calculator will be available to examinees taking the Middle School Education: Mathematics test.

## NUMBER AND OPERATIONS

0001 Understand numbers.
For example:
1.1 Analyze the relationships between the subsets of the real numbers.
1.2 Understand the role of place value in any number system.
1.3 Analyze the use of estimation in a variety of situations.
1.4 Translate between different representations of numbers.
1.5 Apply number-theory concepts (e.g., divisibility rules, prime factorization, greatest common factors) in problem-solving situations.

0002 Understand operations.
For example:
2.1 Analyze relational and operational properties (e.g., multiplication and division of fractions).
2.2 Analyze a variety of conventional and alternative algorithms.
2.3 Solve a variety of real-life and mathematical problems involving integers, fractions, and decimals, including exponents.
2.4 Solve a variety of real-life and mathematical problems involving ratios, proportions, unit rates, and percents.

## ALGEBRA AND FUNCTIONS

0003 Understand patterns, relations, and functions.
For example:
3.1 Analyze patterns and relationships.
3.2 Analyze the properties of relations and functions in multiple representations (e.g., tables, graphs, equations, words).
3.3 Analyze direct and inverse proportional relationships.
3.4 Determine the effects of transformations on the graph of a function or relation.

## FIELD 012: MIDDLE SCHOOL EDUCATION: MATHEMATICS TEST FRAMEWORK

0004 Understand algebraic techniques and applications.
For example:
4.1 Manipulate algebraic expressions, equations, and inequalities (e.g., simplify, transform, factor).
4.2 Solve linear and nonlinear equations and inequalities.
4.3 Create algebraic expressions or equations that describe numbers or relationships.

Understand linear relations and applications.
For example:
5.1 Analyze the relationship between a linear equation or inequality and its representations.
5.2 Solve systems of linear inequalities or equations with a variety of methods.
5.3 Interpret the meaning of the slope and the $y$-intercept in various contexts.
5.4 Analyze a variety of real-life and mathematical problems involving linear equations, systems, and inequalities

Understand nonlinear relations and concepts of calculus.
For example:
6.1 Analyze relationships between multiple representations of a nonlinear equation (e.g., quadratic, polynomial, exponential) or inequality.
6.2 Solve a variety of real-life and mathematical problems involving nonlinear equations and inequalities.
6.3 Demonstrate knowledge of the concepts of limit, continuity, and rate of change as they relate to function behavior.
6.4 Demonstrate knowledge of sequences and series and of recursive definitions.
6.5 Demonstrate knowledge of how concepts of calculus can be used to solve problems in real-life situations.

## FIELD 012: MIDDLE SCHOOL EDUCATION: MATHEMATICS TEST FRAMEWORK

## MEASUREMENT AND GEOMETRY

0007 Understand measurement principles, procedures, and applications.
For example:
7.1 Reason quantitatively and use units and unit conversions to solve problems.
7.2 Calculate or estimate measures of lengths, areas, and volumes.
7.3 Apply the concepts of similarity, scale factors, and proportional reasoning to solve indirect measurement problems.
7.4 Analyze precision, accuracy, and rounding in measurements and computed quantities.

0008 Understand Euclidean geometry in two and three dimensions.
For example:
8.1 Analyze properties of points, lines, planes, and angles.
8.2 Use the properties of triangles, quadrilaterals, and other polygons and circles to solve problems.
8.3 Apply principles of similarity and congruence.
8.4 Understand and apply the Pythagorean theorem and its converse.
8.5 Visualize relationships between two-dimensional and threedimensional figures.
8.6 Analyze geometric arguments using deductive reasoning.

0009 Understand coordinate and transformational geometry.
For example:
9.1 Analyze two- and three-dimensional figures using coordinate systems.
9.2 Connect algebra and geometry by applying concepts of distance, midpoint, and slope to classify figures and solve problems in the coordinate plane.
9.3 Analyze transformations of figures in the coordinate plane.
9.4 Analyze figures in terms of symmetry and tessellations of the plane.

## FIELD 012: MIDDLE SCHOOL EDUCATION: MATHEMATICS TEST FRAMEWORK

## STATISTICS AND PROBABILITY

0010 Understand principles and techniques of statistics.
For example:
10.1 Analyze the effects of bias and sampling techniques.
10.2 Use appropriate formats for organizing and displaying data.
10.3 Analyze univariate and bivariate data in a variety of representations.
10.4 Make inferences and justify conclusions from data presented in a variety of representations.
10.5 Analyze the use of measures of central tendency and spread.

0011 Understand principles of probability and techniques for determining probability.

For example:
11.1 Determine probabilities of simple and compound events.
11.2 Use counting principles (e.g., permutations, combinations) to calculate probabilities and solve problems.
11.3 Use a variety of visual representations to calculate probabilities.
11.4 Demonstrate knowledge of methods for simulating probabilities.

